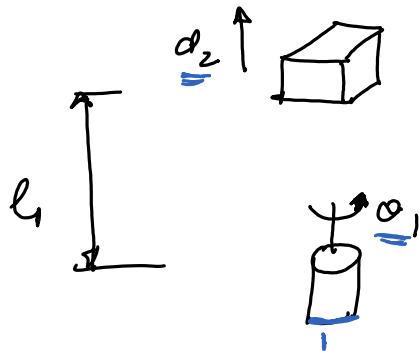


(2) Example 2: 3-link manipulator

1R-2P



• end-effector

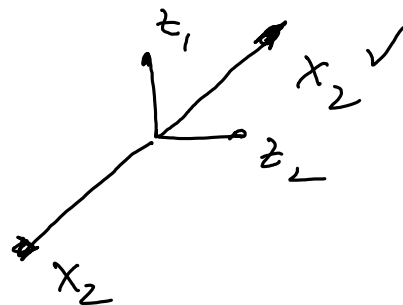
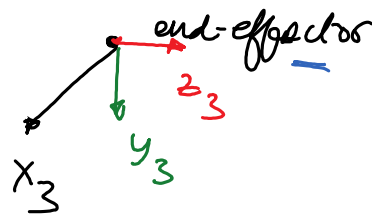
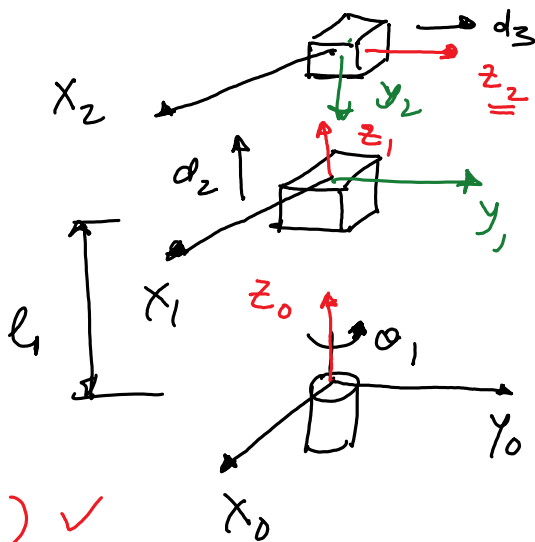


→ only joints are shown

→ links connect the joints

Find the position and orientation of the end-effector

(1)



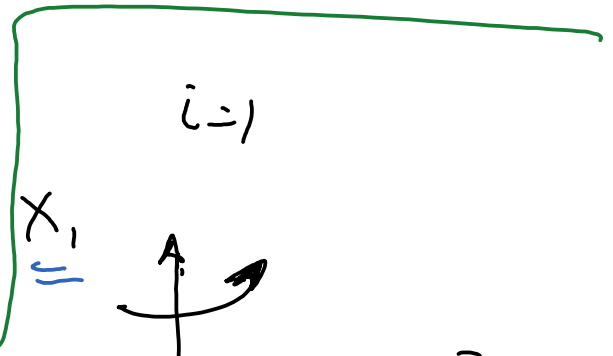
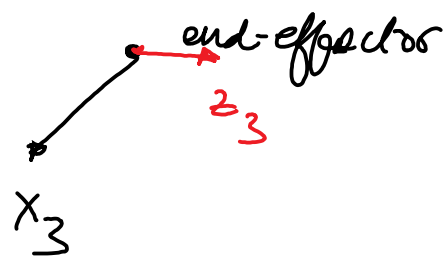
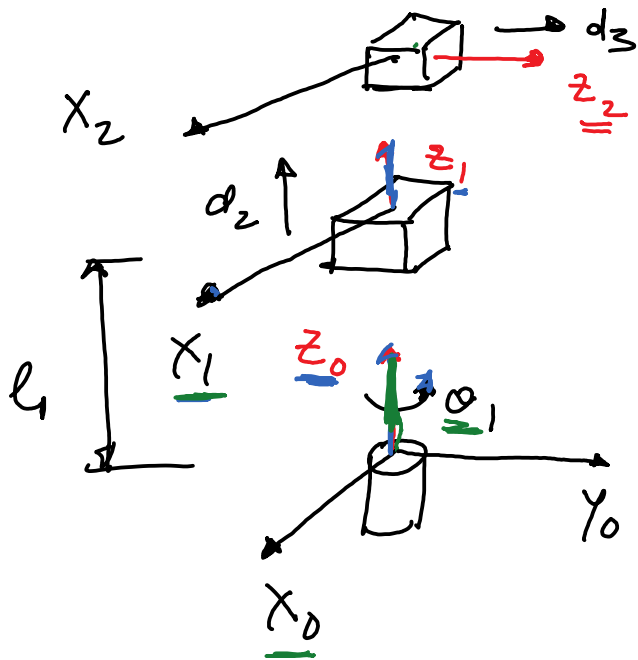
(a) ✓

(b) ✓

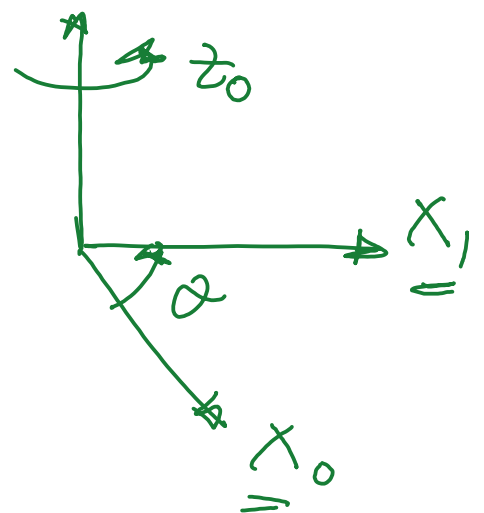
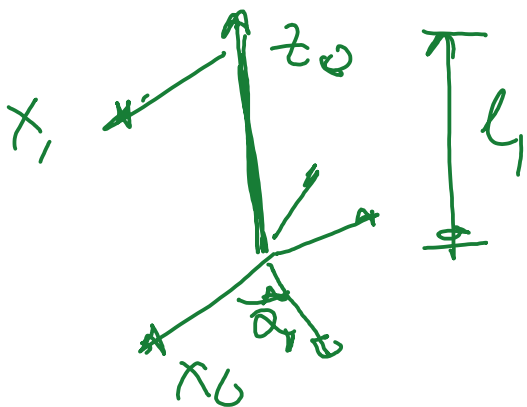
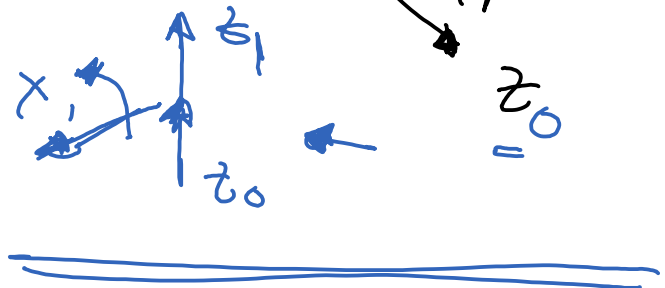
(c) z_0 & z_1 (ii)

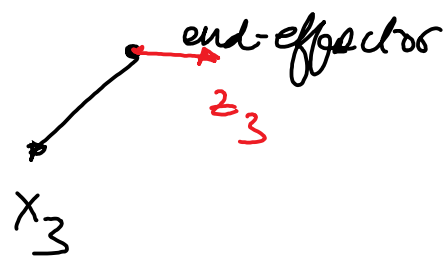
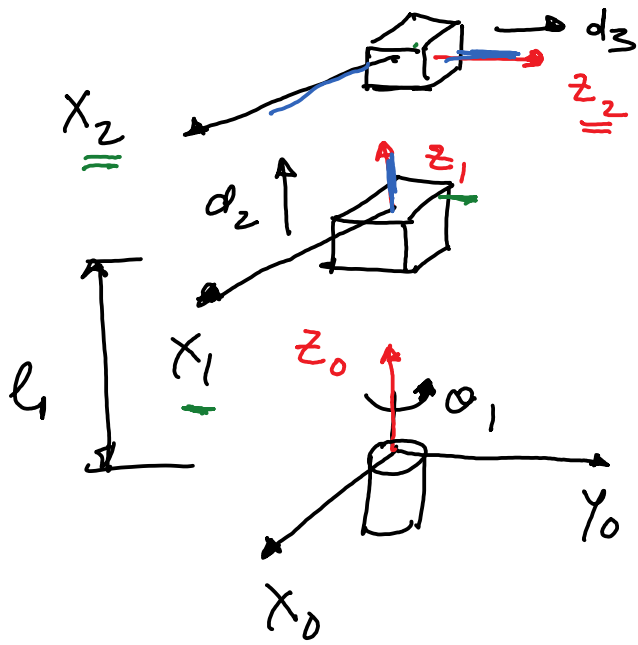
z_1 & z_2 (iii)

(d) (c) (iii)



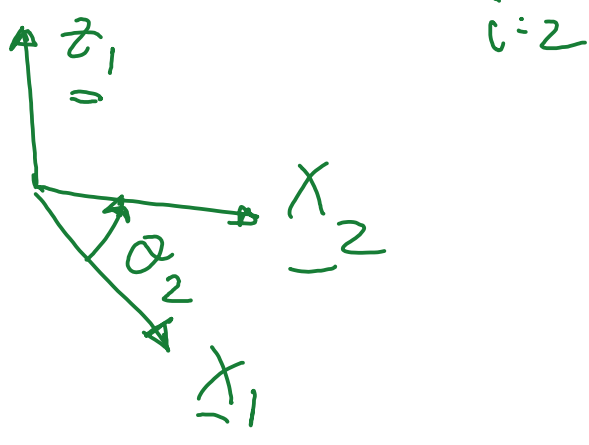
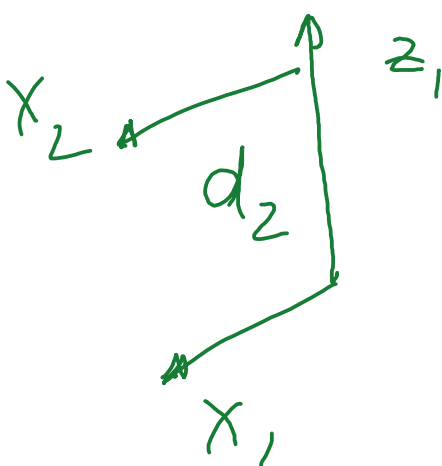
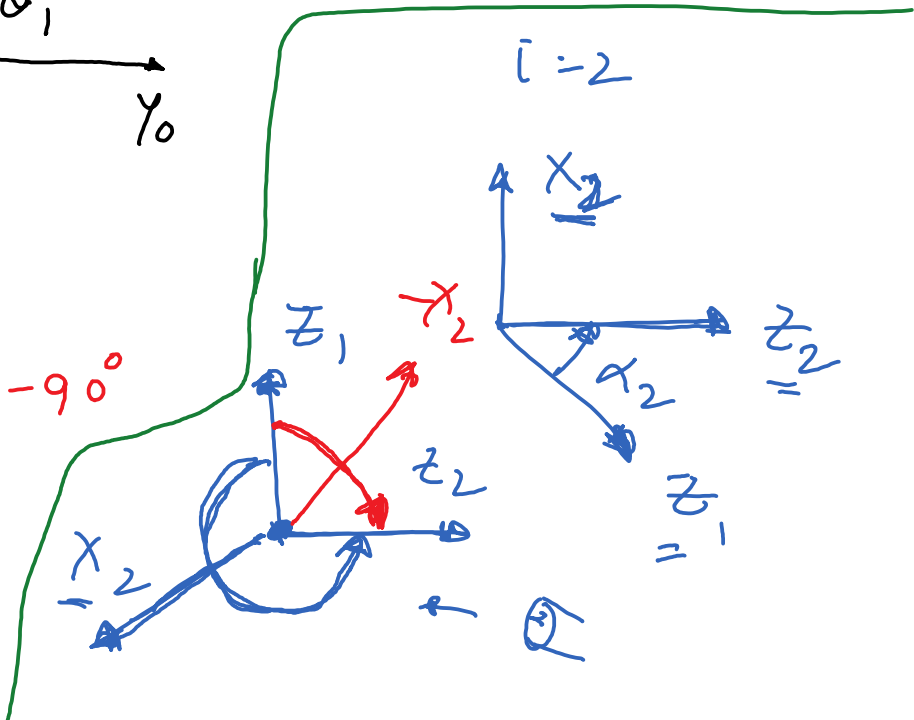
$\underline{a}_1 = 0$
 $\alpha_1 = \theta_1$
 $d_1 = l_1$
 $\alpha_1 = \theta_1$ (controlled)

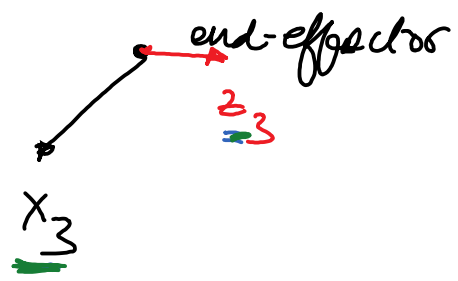
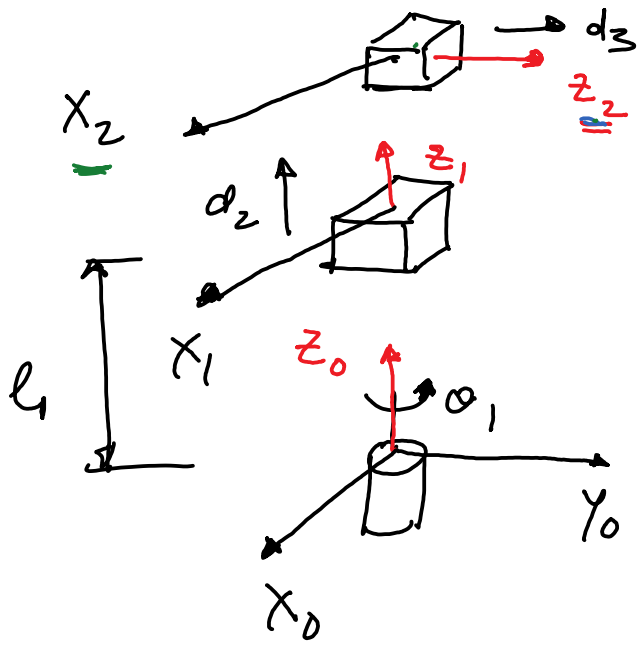




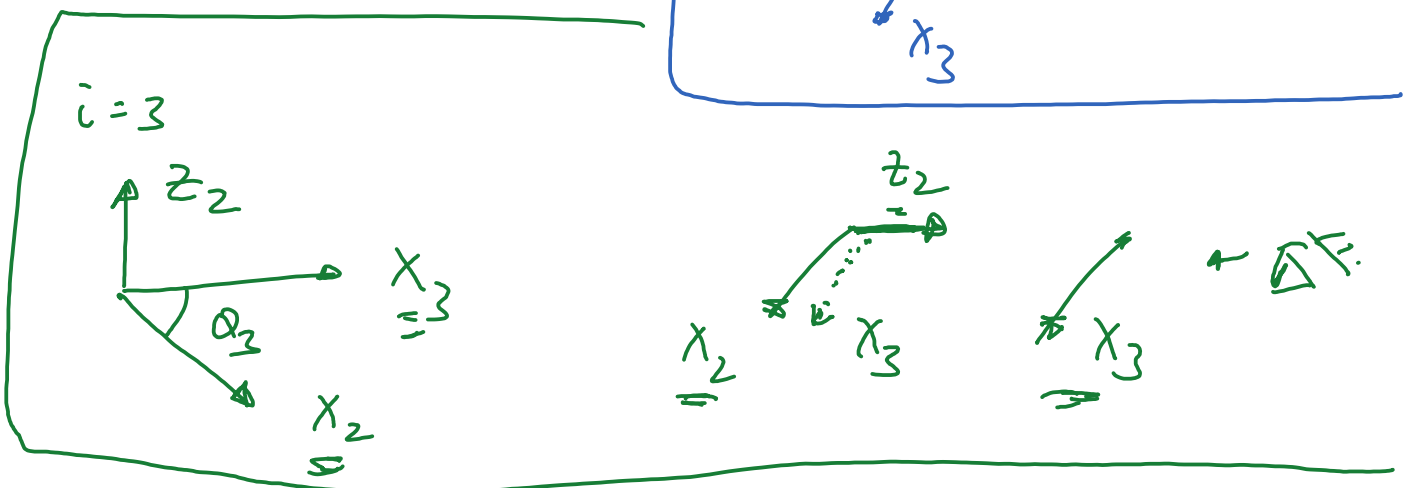
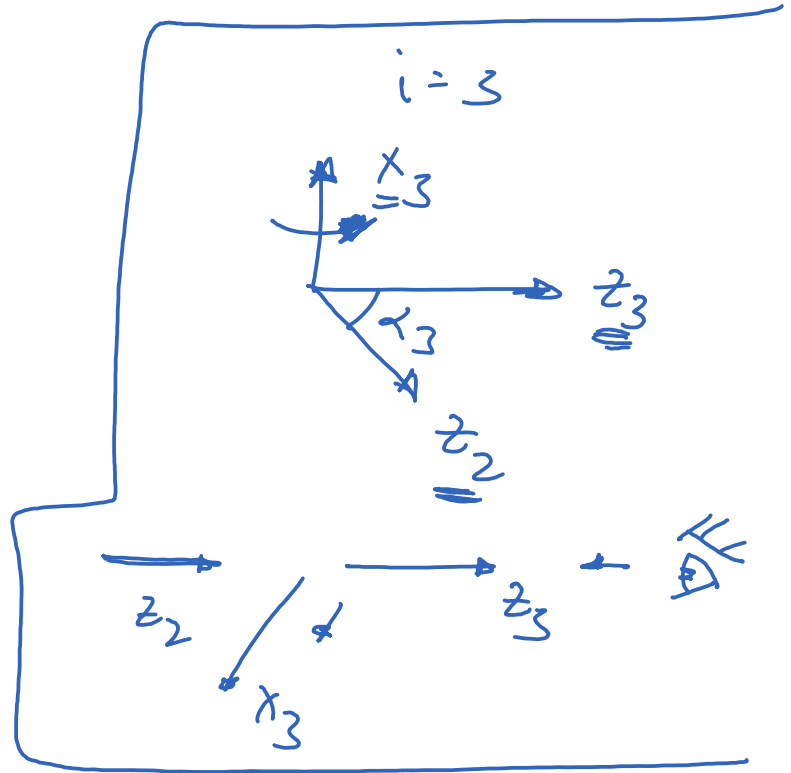
$\vec{a}_2 = 0$
 $\alpha_2 = 270^\circ$
 $d_2 = d_2$
 $\theta_2 = \odot$

-90°





$$\begin{aligned}
 a_3 &= 0 \\
 \alpha_3 &= 0 \\
 d_3 &= d_3 \\
 \theta_3 &= 0
 \end{aligned}$$



Link i	a_i	α_i	d_i	θ_i
1	0	0	l_1	θ_1
2	0	$270^\circ / -90^\circ$	d_2	0
3	0	0	d_3	0

(3) $H_{i-1}^i = \begin{bmatrix} \dots & \dots & \dots & \dots \end{bmatrix}$ see DH handout

H_0^1, H_1^2, H_2^3
 $i=1, i=2, i=3$

$$H_3^0 = H_1^0 H_2^1 H_3^2 = \begin{bmatrix} c_1 & 0 & -s_1 & -s_1 d_3 \\ s_1 & 0 & c_1 & c_1 d_3 \\ 0 & 1 & 0 & l_1 + d_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

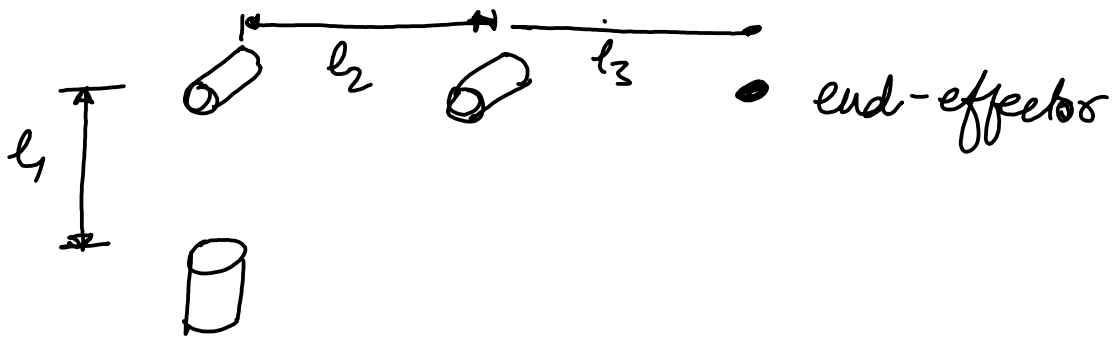
Position of end-effector: $\begin{bmatrix} -s_1 d_3 \\ c_1 d_3 \\ l_1 + d_2 \end{bmatrix}$

→ Orientation of end-effector = $\begin{bmatrix} c_1 & 0 & -s_1 \\ s_1 & 0 & c_1 \\ 0 & 1 & 0 \end{bmatrix}$

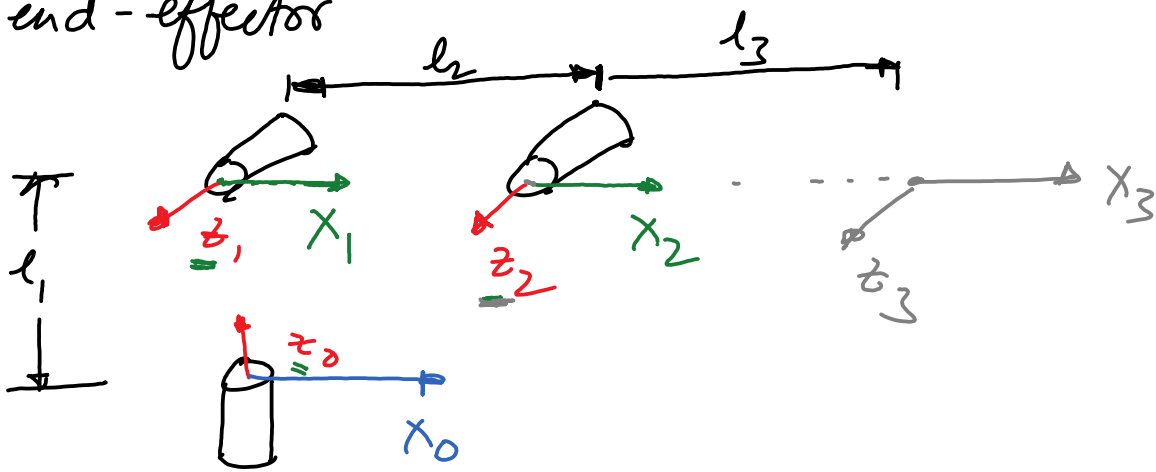
$c_1 = \cos \theta_1, \quad s_1 = \sin \theta_1$

convert to 3-2-1 euler angles.

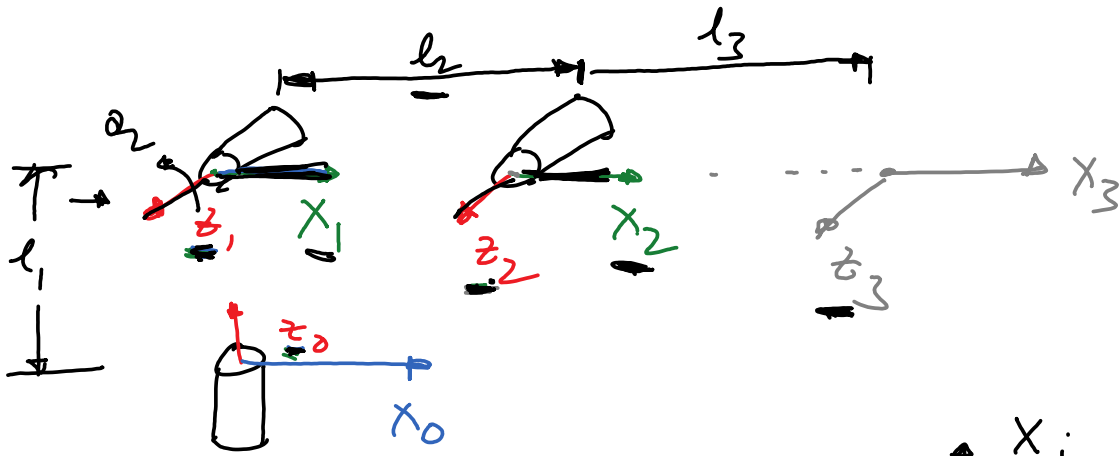
(3) Example 3 3R manipulators



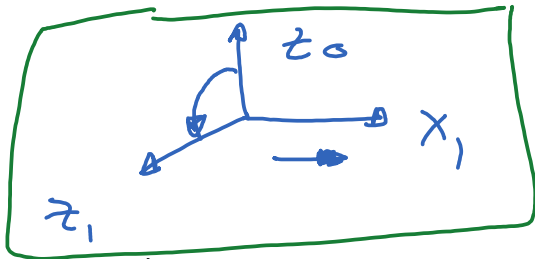
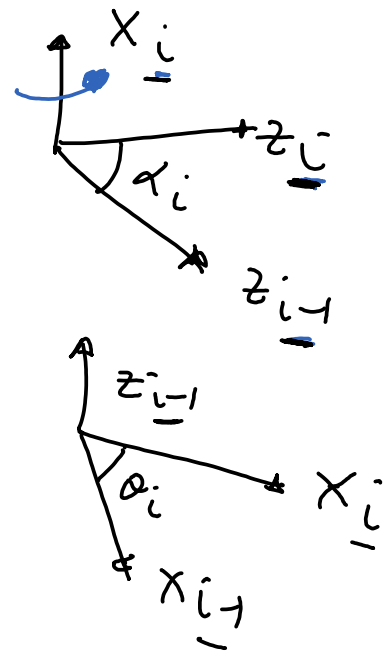
Find the position & orientation of the end-effector



- 1 (a) (b), (c) (iii) z_0 & z_1 } (d) - (c) (i)
 (ii) z_1 & z_2 }



Link	a_i	α_i	d_i	θ_i
1	0	90°	l_1	α_1
2	l_2	0	0	α_2
3	l_3	0	0	α_3



$$(3) \quad H_i^0 = \begin{bmatrix} - & & & \\ - & & & \\ - & & & \\ - & & & \end{bmatrix}$$

$$H_1^0, H_2^1, H_3^2 \quad \leftarrow \quad i=1, 2, 3.$$

$$H_3^0 = H_1^0 H_2^1 H_3^2 = \begin{bmatrix} R_3^0 & d_3^0 \\ 0 & 1 \end{bmatrix}$$

do this computation symbolically in MATLAB.

pos, hion = d_3^0
orientation = R_3^0