

# MuJoCo: double pendulum (I)

## Overview

- I. Create a doublependulum model in xml
2. Check energy balance of a free pendulum
3. Check equations of motion
4. Torque-based position control using three methods
  - i) position-derivative (PD) control
  - ii) (gravity + coriolis forces) + PD control
  - iii) feedback linearization control
5. Writing data file from MuJoCo and plotting in MATLAB

# MuJoCo: double pendulum (2)

Using [template\\_writeData.zip](#) to get started

- I. From [tiny.cc/mujoco](#) download template\_writeData.zip and unzip in myproject
2. Rename folder template to dbpendulum
3. Rename pendulum.xml to doublependulum.xml
4. Make these three changes
  - I. main.c — line 28, change template\_writeData/ to dbpendulum/ and pendulum.xml to doublependulum.xml
  2. makefile — change ROOT = template\_writeData to ROOT = dbpendulum also UNCOMMENT (remove #) appropriate to your OS
  3. run\_unix / run\_win.bat change <template\_writeData> to <dbpendulum>
5. In the \*shell, navigate to dbpendulum and type ./run\_unix (unix) or run\_win (windows); \*shell = terminal for mac/linux and x64 (visual studio) for win

# MuJoCo: double pendulum (3)

Main.c

## I) Check energy

- `mj_energyPos(m,d) & mj_energyVel(m,d);`

# MuJoCo: double pendulum (4)

## Main.c

2) Check equations of motion:  $\mathbf{M} \dot{\mathbf{q}} + \mathbf{C} + \mathbf{G} = \tau$

- $\mathbf{M}$  is mass matrix  $2 \times 2$
- $\dot{\mathbf{q}}$  is acceleration,  $2 \times 1$
- $\mathbf{C}$  is coriolis forces,  $2 \times 1$
- $\mathbf{G}$  is gravitational force,  $2 \times 1$
- $\tau$  is external torque,  $2 \times 1$

# MuJoCo: double pendulum (5)

## Main.c

2) Check equations of motion:  $M \ qddot + C + G = \tau$

MuJoCo equations of motion:

$$M \ qacc + qfrc\_bias = qfrc\_applied + ctrl$$

- $qfrc\_bias = C + G$
- $\tau$  can be  $qfrc\_applied$  OR  $ctrl$
- $qfrc\_applied$  is always available (generalized force)
- $ctrl$  is available on if an actuator is defined

# MuJoCo: double pendulum (6)

Main.c

Equations:  $\mathbf{M} \ddot{\mathbf{q}} + \mathbf{f} = \tau$  where  $\mathbf{f} = \mathbf{C} + \mathbf{G}$

## 3) Controllers

### i) Proportional-Derivative control

$$\tau = -K_p(q - q_{\text{ref}}) - K_d \dot{q}$$

### ii) (gravity + coriolis forces) + PD control

$$\tau = \mathbf{f} - K_p(q - q_{\text{ref}}) - K_d \dot{q}$$

### iii) Feedback linearization

$$\tau = \mathbf{M}(-K_p(q - q_{\text{ref}}) - K_d \dot{q}) + \mathbf{f}$$