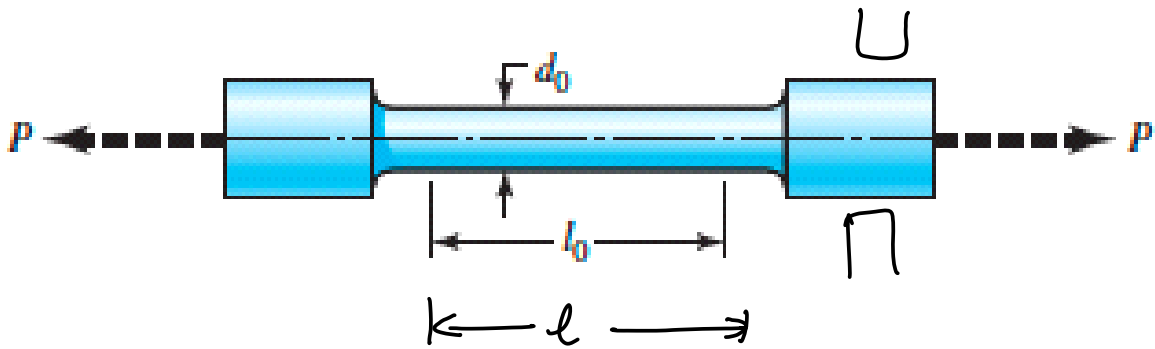


specimen

Material strength and stiffness



Instron \rightarrow changes as $P \uparrow$

P - external load
 l_0 - gauge length
 d_0 - diameter

Stress

$$\sigma = \frac{P}{A} = \frac{P}{(\pi d^2/4)} = \frac{4P}{\pi d^2}$$

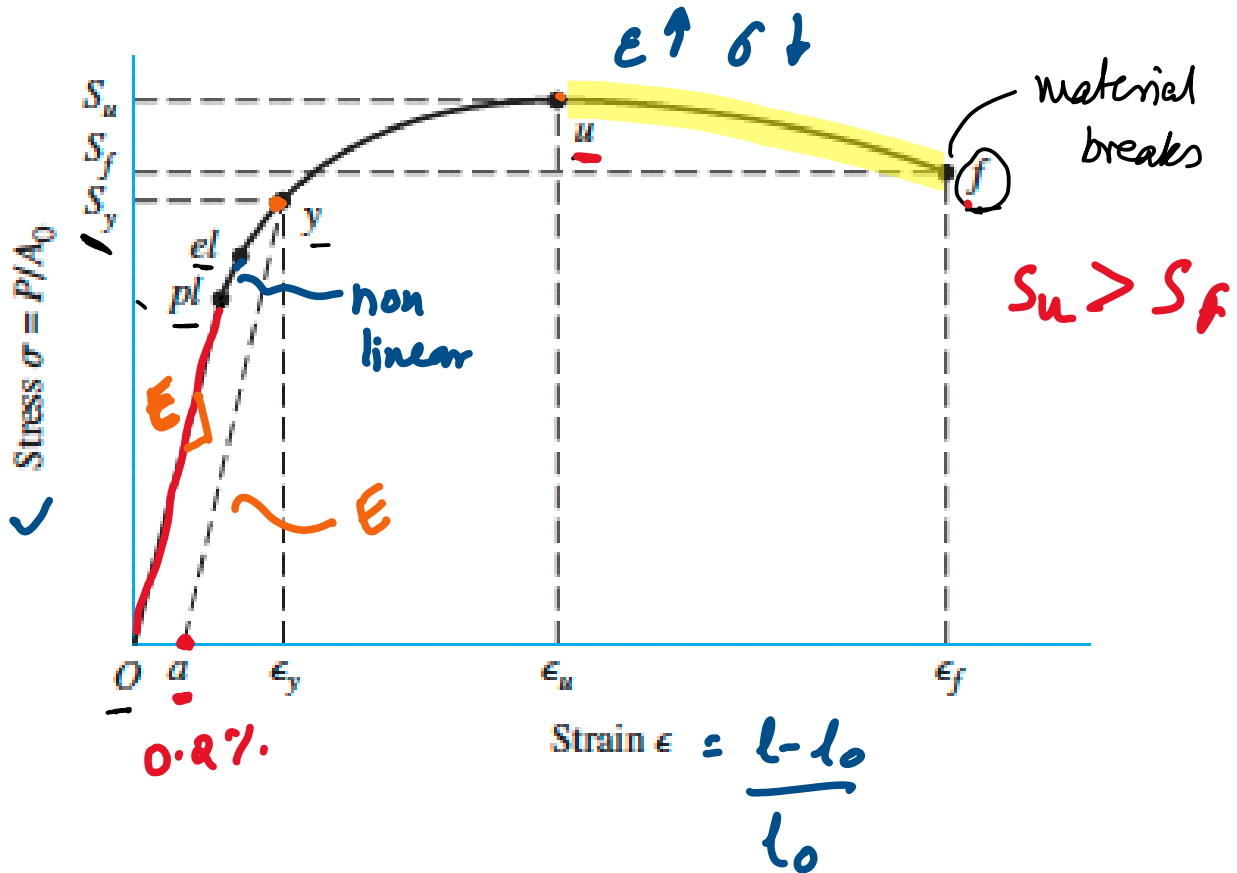
Engineering Strain

$$\epsilon = \frac{l - l_0}{l_0} = \frac{\Delta l}{l_0}$$

$P \uparrow$ $l \uparrow$ $d \downarrow$ $\epsilon \uparrow$



ductile (metals)



(i) pl - proportional limit. This is the point upto which the σ - ϵ curve is linear

(ii) el - elastic limit

from pl - el system is non-linear

Beyond el , the material becomes plastic. That is, when P is reduced to zero, it does not go back to its original length l_0

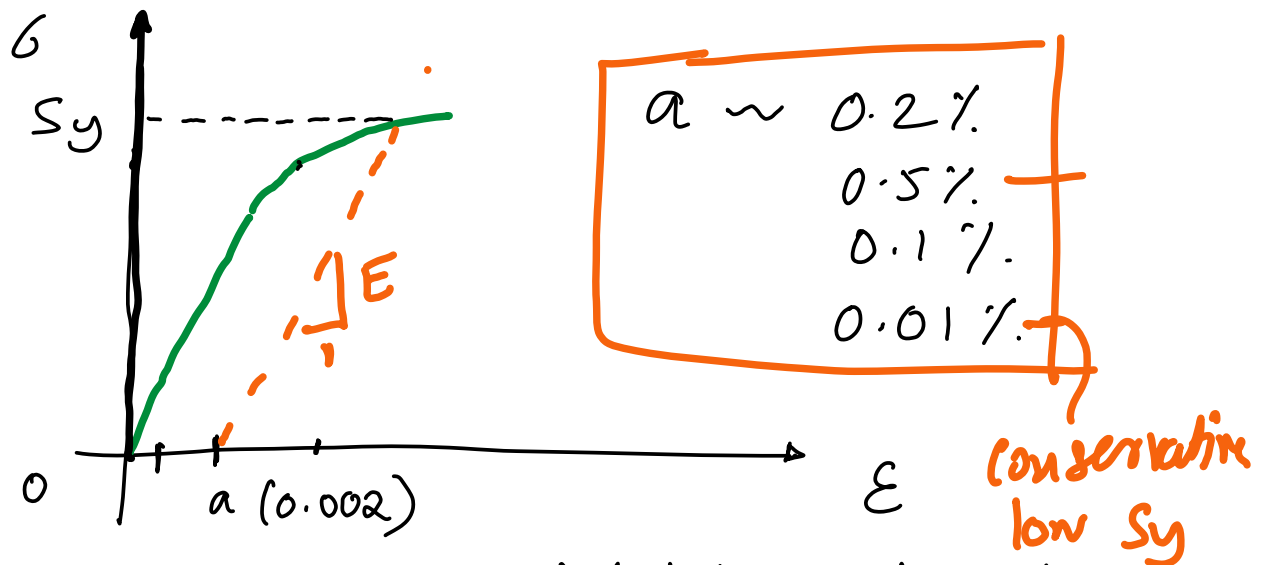
y : yield point

el-y : the strain increases faster than the stress

stress at 'y' is called the yield strength S_y

important design number.

An offset method is used to compute S_y



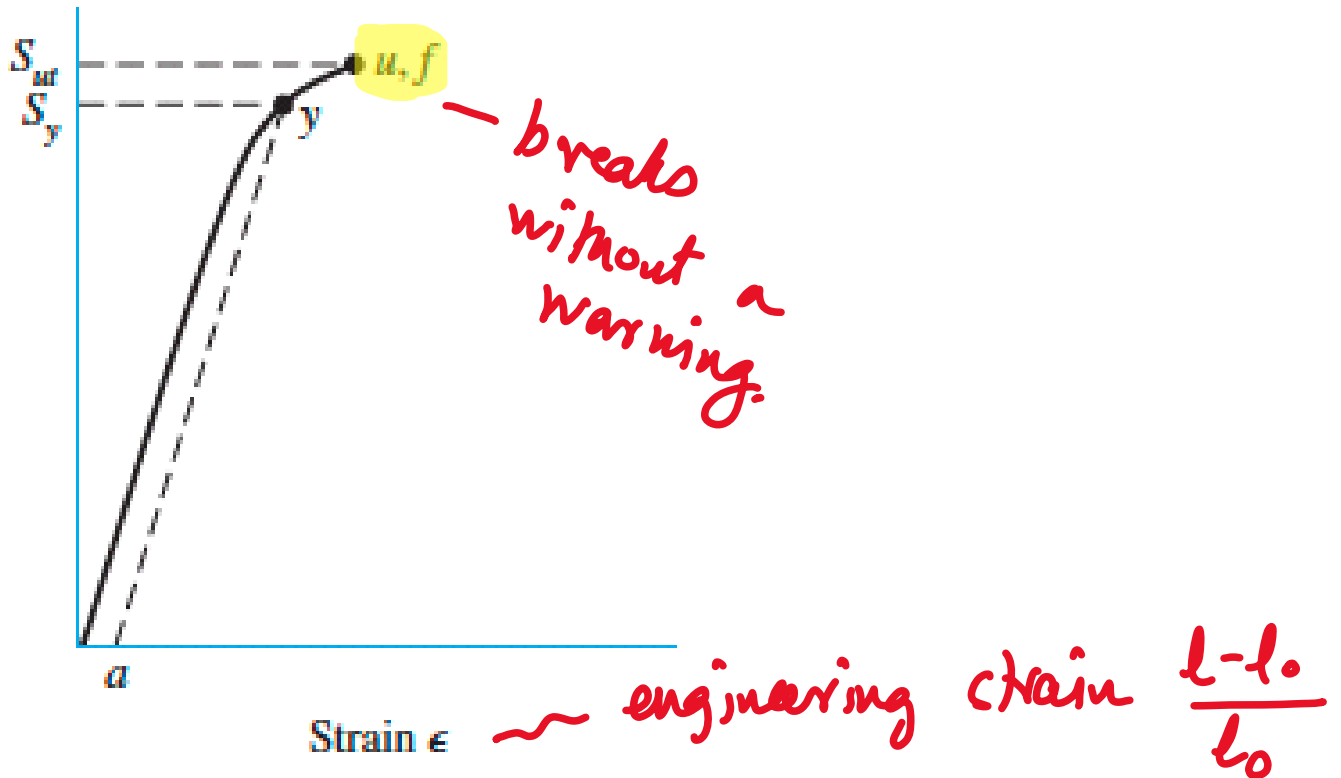
- ① Assume an offset point 'a' to be at 0.2% (= 0.002)
- ② Draw a straight line from 'a' with a slope of E
- ③ The point of intersection of this line with the σ - ϵ curve is S_y

with the σ - ϵ curve is S_y

(iv) u - ultimate or maximum strength
 S_u

(v) f - fracture point / material breaks

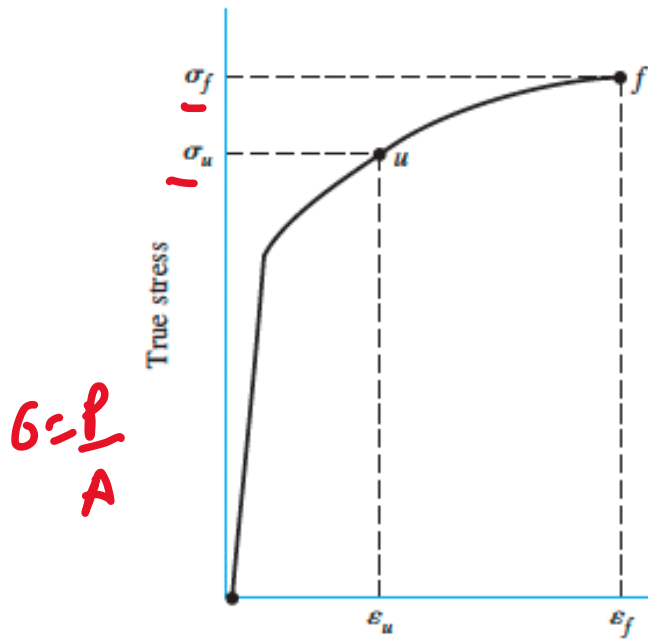
brittle (ceramic, glass, graphite)



The behavior of a brittle material is similar to a ductile material upto point y

u, f are the same points. Here the material breaks / fractures

True stress-strain



$$\left. \begin{aligned} \sigma_f &> \sigma_u \\ S_u &> S_f \end{aligned} \right\}$$

$$\text{true strain} = \ln\left(\frac{l}{l_0}\right)$$

$$\epsilon_t = \int_{l_0}^l \frac{dl}{l} = \ln l \Big|_{l_0}^l = \ln\left(\frac{l}{l_0}\right)$$