

Find $\underline{v_x, v_y}$ such that the ball hits the target

① $[t, x] = \underline{\text{ode45}}$ ('rhs', x_0 , options)

options = ('events', @target)

target $\left\{ \begin{array}{l} \text{value} \\ \text{isterminal} \\ \text{direction} \end{array} \right. = \left. \begin{array}{l} x_{\text{interact}} - x_c = 0 \\ \underline{y_{\text{interact}} - y_c = 0} \end{array} \right\}$

function does not know this

here time is implicit

fmincon \rightarrow needs gradients $\frac{\text{d constraints}}{\text{optimization variables}}$

$\rightarrow \left\{ \frac{\partial x_c}{\partial v_x}, \frac{\partial y_c}{\partial v_x}, \frac{\partial x_c}{\partial v_y}, \frac{\partial y_c}{\partial v_y} \right\}$

are non-smooth.

Makes the problem non-smooth & fmincon has a hard time converging

$$\textcircled{2} (t, x) = \text{ode45}(\text{'rhs'}, x_0, \text{options})$$

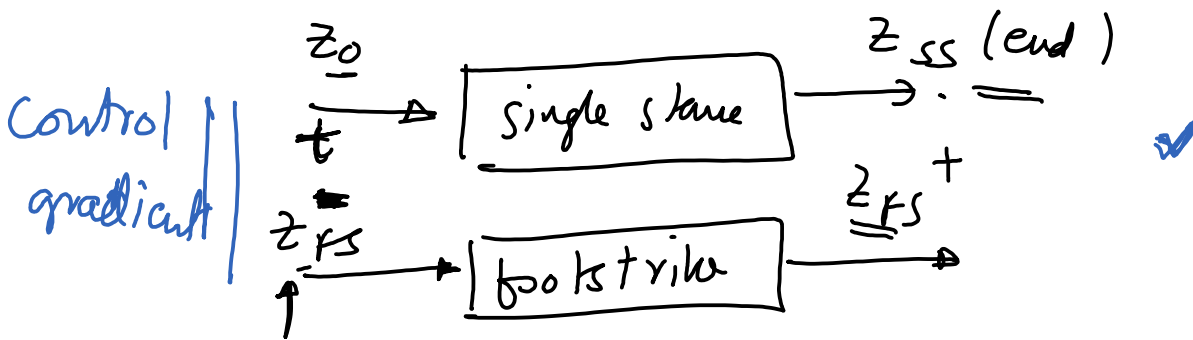
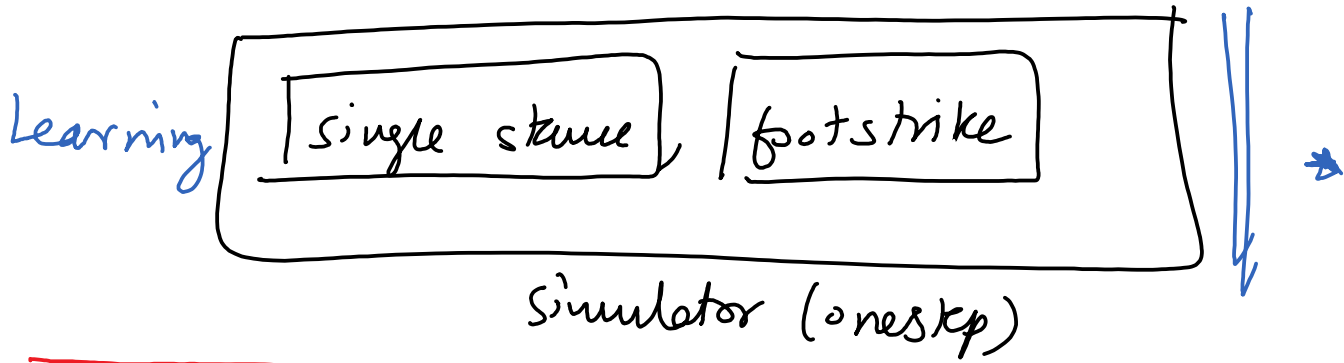
options \rightarrow do not specify event

t = integration time as a free parameter

optimization variables v_x, v_y, t

$$\text{constraints} = \left. \begin{aligned} x_{\text{int}} - x_c &= 0 \\ y_{\text{int}} - y_c &= 0 \end{aligned} \right\}$$

Legged optimization



optimization variable z_0, t, z_{fs}

constraints. $z_1 = z_{ss}(\text{end}) - z_{fs} = 0$
 $z_2 = z_{fs}^+ - z_0 = 0$ } constraints explicit

function \rightarrow

$$\left. \begin{array}{l} \frac{\partial z_1}{\partial z_0}, \frac{\partial z_1}{\partial z_{fs}}, \frac{\partial z_1}{\partial t} \\ \frac{\partial z_2}{\partial z_0}, \frac{\partial z_2}{\partial z_{fs}}, \frac{\partial z_2}{\partial t} \end{array} \right\}$$